



ANSWER BOOK

Capacitors and energy stored

Capacitance · Year 13

AQA 3.7.4.1, 3.7.4.2, 3.7.4.3 · CIE 19.1, 19.2 · OCR A 6.1.1, 6.1.2, 6.2.3

10 questions · 30 marks

NAVY EDITION

SECTION A · Warm-up

- A1** Capacitance is the charge stored per unit potential difference, $C = Q/V$. Its unit is the [2]
farad (F), equal to one coulomb per volt.
- A2** $C = Q/V = (6.0 \times 10^{-3})/12 = 5.0 \times 10^{-4} \text{ F (500 } \mu\text{F)}.$ [2]
- A3** $E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}Q^2/C.$ [2]

SECTION B · Standard

- B1** (a) $Q = CV = 100 \times 10^{-6} \times 20 = 2.0 \times 10^{-3} \text{ C}.$ (b) $E = \frac{1}{2}CV^2 = \frac{1}{2} \times 100 \times 10^{-6} \times 20^2 = 0.020 \text{ J}.$ [3]
- B2** $E = \frac{1}{2}QV = \frac{1}{2} \times 5.0 \times 10^{-3} \times 8.0 = 0.020 \text{ J}.$ [3]
- B3** $C = \epsilon_0 A/d = (8.85 \times 10^{-12} \times 0.020)/(1.0 \times 10^{-3}) = 1.77 \times 10^{-10} \text{ F (177 pF)}.$ [4]
- B4** $Q = CV = 470 \times 10^{-6} \times 9.0 = 4.23 \times 10^{-3} \text{ C}.$ $E = \frac{1}{2}CV^2 = \frac{1}{2} \times 470 \times 10^{-6} \times 9.0^2 = 0.019 \text{ J}.$ [3]

SECTION C · Stretch

- C1** $C = \epsilon_0 \epsilon_r A/d$, which is 4.0 times the vacuum value: $C = 4.0 \times 177 = 708 \text{ pF}.$ At a fixed [4]
voltage $E = \frac{1}{2}CV^2$, so the energy stored also increases by a factor of 4.
- C2** (a) $E = \frac{1}{2}Q^2/C = \frac{1}{2} \times (3.3 \times 10^{-3})^2/(220 \times 10^{-6}) = 0.0247 \text{ J}.$ (b) $V = Q/C = (3.3 \times 10^{-3})/(220 \times 10^{-6}) = 15 \text{ V}.$ [4]
- C3** The field polarises the dielectric: its polar molecules rotate to line up with the field, [3]
producing their own opposing field. This reduces the net field (and so the voltage) for a
given stored charge, so more charge can be held per volt, raising the capacitance.