



ANSWER BOOK

The time constant and exponential decay

Capacitance · Year 13

AQA 3.7.4.4 · CIE 19.3 · OCR A 6.1.3

10 questions · 30 marks

NAVY EDITION

SECTION A · Warm-up

- A1** The time constant is $\tau = RC$. It is the time for the charge (or voltage, or current) to fall to $1/e$ (about 37%) of its initial value during discharge.
- A2** $\tau = RC = 10000 \times 100 \times 10^{-6} = 1.0 \text{ s.}$ [2]
- A3** $Q = Q_0 e^{-t/RC}$, where Q_0 is the initial charge. [2]

SECTION B · Standard

- B1** $\tau = RC = 2200 \times 470 \times 10^{-6} = 1.03 \text{ s.}$ After one time constant the charge has fallen to $1/e$ (37%) of its initial value.
- B2** $\tau = RC = 47000 \times 100 \times 10^{-6} = 4.7 \text{ s.}$ $V = V_0 e^{-t/RC} = 12 \times e^{-5.0/4.7} = 4.14 \text{ V.}$ [4]
- B3** $T_{1/2} = 0.69 \times 4.7 = 3.24 \text{ s.}$ [3]
- B4** $R = \tau/C = 2.0 / (220 \times 10^{-6}) = 9091 \Omega \text{ (9.1 k}\Omega\text{).}$ [3]

SECTION C · Stretch

- C1** $5.0 = 20e^{-t/3.0}$, so $e^{-t/3.0} = 0.25$ and $t = -3.0 \times \ln(0.25) = 4.16 \text{ s.}$ [4]
- C2** $\tau = RC = 10000 \times 470 \times 10^{-6} = 4.7 \text{ s.}$ $V = 9.0 \times (1 - e^{-10/4.7}) = 7.93 \text{ V.}$ [4]
- C3** Taking logs of $V = V_0 e^{-t/RC}$ gives $\ln V = \ln V_0 - t/RC$, a straight line. Its gradient is $-1/RC$, so $RC = -1/\text{gradient}$; the time constant is the negative reciprocal of the slope.